# Curriculum Progression Pathway

# **MATHS**



#### Why is the study of MATHEMATICS important?

MATHEMATICS has two disciplines: Pure and Applied – Pure Mathematics is the abstract science of number, quantity and space as abstract concepts and Applied Mathematics is where the knowledge learned is applied to other disciplines such as statistics, physics and engineering.

Initially your mathematics study focuses on building firm foundations, including your fluency and understanding in readiness for your future GCSE and even A level mathematics study. Our curriculum is carefully designed to ensure that all students get a firm grounding in the basic rules of number. This is differentiated by depth, as opposed to students racing onto the next topic. This approach develops more confident mathematicians as students move through the curriculum and helps them to retain their new learning for longer. Your study of mathematics at Outwood will make you think about the beauty of how numbers connect and how processes relate to each other. Mathematics encourages you to discover those connections for yourself, to make you a detective of mathematics and to explore how to solve problems. This enables you to become an analytical thinker, someone who sees that the answer is only the beginning. It will help you to learn how to make conjectures (a conclusion based on evidence, patterns and thought, but not yet confirmed with proof) to reason and to prove. It will enable you to be more logical in your approach to complex issues and be more analytical.

You will discover how the basic four rules can be applied to fractions, decimals, standard form and algebra and how multiplicative reasoning can be applied to many areas of maths, such as percentages, ratio, proportion and enlargement to name but a few. You will get to investigate the beauty of mathematics connected to shape, and the usefulness it brings in analysing data and solving mechanical problems.

Your study of Mathematics will encourage you to think deeply and help you to problem solve more effectively – a great life skill that all universities and employers will appreciate. Across your study you will explore number, algebra, shape and space and statistics. Lessons will provide a wide range of opportunities for constructing your own learning and discovering your own rules, through the use of concrete materials such as counters, through pictorial representations to demonstrate mathematical concepts and to apply these to solve problems, both abstract and from real-life.

Maths lessons will be full of discussion, questioning, proving and explaining. You are going to love it! Mathematics will expand your mind! Big Questions such as: How tiny is the earth in comparison with the universe? How can solutions to difficult engineering problems be found using graphs and calculus? How do people predict what is going to happen in the economy? and other such seemingly bewildering questions will be answered ... you just need to learn the basics, be an inquisitive learner, and the rest will follow.



# What skills will the study of Mathematics teach you?

You are a citizen in this world and you need to know the basic skills of number and how to apply them to a range of problems – known as 'being numerate'. It will teach you:

- Not to be afraid of "being lost" and having to struggle to find one's way through the problem RESILIENCE!
- To use calculation to solve basic problems
- To make and use generalisations—often quite quickly. One of the basic abilities, easily detectable even at the level of primary school: after solving a single example from a series, a child immediately knows how to solve all examples of the same kind.
- To have rapid and sound memorisation of mathematical material.
- To be able to concentrate on mathematics for long periods without apparent signs of tiredness.
- To be able to offer and use multiple representations of the same mathematical object. (For example, switching easily between representations of the same function by tables, charts, graphs, and analytic expressions.)
- An instinctive tendency to approach a problem in different ways: even if a problem has been already solved, you are keen to find an alternative solution.
- To utilise analogies and make connections.
- Skills to link two (or more) elementary procedures to construct a solution to a multi-step problem.
- To recognise what it means to "know for certain".
- To detect unstated assumptions in a problem, and either to explicate and utilise them, or to reject the problem as ill-defined.
- To be efficient, a distinctive tendency for "economy of thought," striving to find the most economical ways to solve problems, for clarity and simplicity in a solution.
- To be aware of the presence and importance of an underlying structure.
- To use rapid abbreviation, compression or a curtailment of reasoning in problem solving e.g. algebra.
- How to grasp encapsulation and de-encapsulation of mathematical objects and procedures.

How does your study of MATHEMATICS support your study in other subjects?

Study of any subject in our curriculum takes full advantage of links with other subject areas- we term these as interdisciplinary links and we make the most of them because we know that deep learning requires the transference of knowledge and skills from one topic of learning to another. Once you can transfer your learning across topics and subject areas then you are really mastering what you know and how to apply your understanding and skills.

Mathematics touches on many other subjects such as geography and science, any subject that analyses data, looks at trends, uses formulae. Computer Science is a subject that uses the algorithmic approach that many topics in mathematics also use. The ability to follow a process accurately is applicable to many other subjects too. The Social Sciences, particularly at Post 16 and at undergraduate level have a strong need for the use of data, for understanding of exponential growth and decay, for manipulation of formulae – and this is one reason why the Core Maths AS Level was introduced recently.

Across the other subjects, teachers will make reference to your learning in Maths and this will help you to develop your understanding. There may be opportunities to explore the links between science, engineering and mathematics departments in STEM activities.

Outside of Mathematics lessons there are a range of initiatives that can help you deepen your understanding of mathematics such Numeracy Ninjas, Timetable Rock Stars, UKMT Maths Challenge led by Leeds University, Maths Masters – for our elite mathematicians, and online learning programmes such as the wonderful Sparx.

### How are you assessed in MATHEMATICS?

Throughout the 5 year MATHEMATICS course you are assessed using the following assessment objectives which ensure that you can cumulatively build your subject understanding in preparation for future GCSE and A Level study. There are half termly assessment points each year that we term Praising Stars©. For younger years we base our assessment on our subject mapping of the age related expectations across the curriculum, assessing students' performance at their current stage of study against expectation. At GCSE we make informed predictions informed by our holistic assessment of their progress against the key assessment objectives and their aspirational GCSE targets. These are also the basis for any appropriate support and intervention.

### **Key Assessment Objectives**

## AOI: Use and apply standard techniques

Students should be able to:

- accurately recall facts, terminology and definitions
- use and interpret notation correctly
- accurately carry out routine procedures or set tasks requiring multi-step solutions

## AO2: Reason, interpret and communicate mathematically

Students should be able to:

- make deductions, inferences and draw conclusions from mathematical information
- construct chains of reasoning to achieve a given result
- interpret and communicate information accurately
- present arguments and proofs
- assess the validity of an argument and critically evaluate a given way of presenting information

# AO3: Solve problems within mathematics and in other contexts

Students should be able to:

- translate problems in mathematical or non-mathematical contexts into a process or a series of mathematical processes
- make and use connections between different parts of mathematics
- Interpret results in the context of the given problem
- evaluate methods used and results obtained
- evaluate solutions to identify how they may have been affected by assumptions made

#### GCSE specifications in mathematics should enable students to:

- I. develop **fluent** knowledge, skills and understanding of mathematical methods and concepts
- 2. acquire, select and apply mathematical techniques to solve problems
- 3. reason mathematically, make deductions and inferences and draw conclusions
- 4. comprehend, interpret and communicate mathematical information in a variety of forms appropriate to the information and context.

## How can Mathematics support your future?

We offer the study of GCSE Mathematics and we strongly encourage your continued study in this fantastic subject if you have demonstrated a passion for it, a flair and an ability.

However, whether you have chosen to study Mathematics into A level or not you will have gained a lot from its study over the 5 years from years 7-11. We know that the depth of understanding we encourage and support you to achieve will set you up well to be not only numerate, but a really logical and analytical thinker, who is resilient and ready to solve problems.

Mathematics is offered at prestigious universities either as a single honours or a joint honours subject studied alongside other disciplines e.g. Statistics, Computer Science, Science, Philosophy, Engineering.

A high level of qualification in mathematics is a prerequisite for honours degrees in many engineering and physics related subjects.

It is also cited that an A level in maths demonstrates the very high level of analytical thinking that many universities are looking for in their applicants. The very fact that you have been able to study mathematical thinking post 16 will help your future applications be they for colleges, universities, apprenticeships or employment.

A strong GCSE in Maths opens doors for your future career – employers look favourably on this and it would put you in a very strong position when looking for jobs or placements Post 16 and in colleges.

Careers that the study of MATHEMATICS supports include:

- Actuarial analyst
- Actuary
- Chartered accountant
- Chartered certified accountant
- Data analyst
- Data scientist
- Investment analyst
- Research scientist (maths)
- Secondary school teacher
- Software engineer
- Statistician
- Civil Service fast streamer
- Financial manager
- Financial trader
- Insurance underwriter
- Meteorologist
- Operational researcher
- Quantity surveyor
- Software tester

	7	8	9
Autumn I	UNIT 0 - Introduction to Statistics  Transition project covering: - Collecting and organising data - Construct statistical diagrams including an introduction to Venn Diagrams UNIT I Solve word problems (add and subtract) Ia. Place value (including decimals) inc. multiplying and dividing by positive powers of 10. Place Value NS Ib. Conversion between metric units of measurements 2. Add and subtract (including decimals) Number bonds NS 3. Rounding and Estimating	UNIT 6 Percentages & statistics I. Proportional Reasoning I Proportion NS 2. Convert FDP Basic FDP NS 3. Ordering FDP & equivalence 4. Percentage of an amount 5. Find the whole, given the part and the percentage 6. Interpret and compare statistical representations. 7. Averages and the range incl. frequency tables	UNIT 9 2-D geometry 3. Conversion between length units and between area units 4. Area of trapeziums 5. Areas and perimeters of composite figures UNIT 10 Proportion & Percentages 1. FDP of amounts

	UNIT I		- 2012
	Solve word problems		
	(add and subtract)	UNIT 7	UNIT 10
	4. Perimeter	Number	Proportion & Percentages
	UNIT 2	I. Primes and indices	2. Amounts as percentages
	Explain & Investigate	2. Basic laws of indices	3. Percentage Increase and Decrease
Autumn 2	(multiply and divide)	3. Basic introduction to Surds and four operations	4. Reverse Percentages
	<ol> <li>Factors, HCF, multiples, LCM</li> </ol>	4. Prime Factorisation to find LCM, HCF, squares, cubes	UNIT II
	<ol><li>Venn Diagrams and sets</li></ol>	5. Standard Form	Probability and Statistics
	3. Multiply and divide (including decimals)	Powers of 10 NS	I. Probability
	4. Area of rectangles, triangles and	6. Add and subtract fractions with different denominators	2. Averages from grouped data
	parallelograms		73. 1.1
	5. Calculate the mean		
	UNIT 2		
	Explain & Investigate		
	(multiply and divide)		
	5. Calculate the mean		
	UNIT 3		UNIT I I
	Geometry		Probability and Statistics
	<ol> <li>Draw, measure and name angles</li> </ol>	UNIT 8	3. Compare two data sets including stem-and-leaf
	Time NS	Algebraic expressions	diagrams
	2. Find unknown angles (straight lines, at a	<ol> <li>Formulate and evaluate expressions</li> </ol>	4. Scatter graphs, basic correlation and drawing lines of
Spring I	point, vertically opposite, triangles and	2. Linear equations	best fit
	quadrilaterals)	3. Expressions and equations from real- world situations	UNIT 12
	3. Properties of triangles and quadrilaterals	4. Linear sequences: nth term	Proportional Reasoning
	UNIT 4	5. Cartesian coordinates and an introduction to functions	Ratio – equivalence and simplifying
	Fractions		2. Ratio – problem solving
	1. Introduction to fractions NS		3. Proportional Reasoning 2
	<ol><li>Equivalent fractions and ordering</li></ol>		
	Factors NS		
	3. Mixed numbers & improper fractions		
	4. Adding & subtracting same denominators		

		UNIT 9	
	UNIT 4	2-D geometry	UNIT 12
	Fractions	Draw accurate triangles and quadrilaterals	Proportional Reasoning
	5. Fraction of a quantity & multiplying	Measuring lengths NS	4. Maps and scales
	fractions	2. Find unknown angles (incl. parallel lines)	5. Ratio and Rate incl. speed, distance, time and
Spring 2	6. Divide fractions	3. Conversion between length units and between area units	pressure
	UNIT 5	4. Area of trapeziums	6. Constructing pie and interpreting pie charts
	Applications of algebra	5. Areas and perimeters of composite figures	UNIT 13
	<ol> <li>Negative Numbers</li> </ol>	UNIT 10	3-D geometry
	2. Order of operations	Proportion & Percentages	Rounding, significant figures and estimation
		I. FDP of amounts	
	UNIT 5	UNIT 10	77. 77.
	Applications of algebra	Proportion & Percentages	UNIT 13
İ	3. Substitution	2. Amounts as percentages	3-D geometry
	4. Simplify algebraic expressions	3. Percentage Increase and Decrease	2. Circumference and area of a circle
Summer I	5. Sequences (term-to- term, not nth term)	4. Reverse Percentages	3. 3-D shapes & their nets; plans and elevations
	UNIT 6	UNIT I I	4. Volume and surface area of prisms, composite solids,
	Percentages & statistics	Probability and Statistics	pyramids, cones and spheres (with formula and without
	<ol> <li>Proportional Reasoning I</li> </ol>	1. Probability	for pyramids and cones.) and mass, density and volume
	Proportion NS	2. Averages from grouped data	
	UNIT 6	UNIT I I	
	Percentages & statistics	Probability and Statistics	UNIT 13
	2. Convert FDP	2. Averages from grouped data	3-D geometry
	Basic FDP NS	3. Compare two data sets including stem-and-leaf diagrams	5. Pythagoras – 2-D and 3-D Pythagoras
	<ol><li>Ordering FDP &amp; equivalence</li></ol>	4. Scatter graphs, basic correlation and drawing lines of best	UNIT 14
Summer 2	4. Percentage of an amount	fit	Algebraic Expressions
Summer 2	5. Find the whole, given the part and the	UNIT 12	Sequences including arithmetic & geometric
	percentage	Proportional Reasoning	Expansion incl. double brackets
	6. Interpret and compare statistical	I. Ratio – equivalence and simplifying	Expansion lies, double brackets and solving simple
	representations.	2. Ratio – problem solving	quadratic equations
	7. Averages and the range incl. frequency tables	3. Proportional Reasoning 2	qualitatio equations

	nits 14 to 27 as detailed below. Due to our Covid recovering there will be some flexibility with the timings of when	
UNIT 14  Algebraic Expressions  1. Basic laws of indices and introduction to surds and four operations  2. Sequences including arithmetic & geometric  3. Expansion incl. double brackets  4. Factorisation incl. double brackets and solving simple quadratic equations  5. Algebraic manipulation (rearranging and advance rearranging)	UNIT 15 Graphs and Proportion  1. Cartesian coordinates and an introduction to functions 2. Linear graphs 3. Direct and inverse proportion 4. Relationships and Proportionality 5. Variation and variation with powers (direct and inverse proportion with algebra)	UNIT 16 2-D Geometry 1. Bearings 2. Further construction and loci 3. Congruence and similarity 4. Triangles and quadrilaterals (angles on diagonals) 5. Angles in polygons
UNIT 17 Equations and Inequalities  1. Construct and solve equations and inequalities  2. Graphical solutions to simultaneous linear equations  3. Linear simultaneous equations  4. Quadratic and non-linear graphs and links with quadratic equations	UNIT 18 Sampling and Probability  1. Populations and samples; capture/recapture 2. Theoretical and experimental probability 3. Listing and the product rule for counting 4. Set notation & Venn diagrams 5. Combined events, including tree diagrams and conditional probability	UNIT 19 Geometry  1. Transformations (translation, rotation, reflection) and combined transformations  2. Use known angle and shape facts to obtain simple proofs  3. Enlargement and negative scale factors of enlargement.  4. Combine transformations

# UNIT 20 Geometry

- 1. Similar shapes
- 2. Exploring trigonometric ratios with 30-60-90 and 45-45-90 triangles of varying dimensions (\*not sin,cos,tan)
- 3. Trigonometry and Pythagoras in right angled triangles, 3-D trigonometry and Pythagoras

# UNIT 21

#### Number

- I. Calculations with and rules of indices and fractional indices
  - 2. Indices and Surds
  - 3. Calculations with standard form
- 4. Repeated change and percentage/fraction problems
  - 5. Standard non-linear sequences and recurrence relations and iteration

# UNIT 22 Statistics

- I. Represent and describe distributions and histograms, cumulative frequency and box plots
  - 2. Identify misleading graphs
    - 3. Time series
  - 4. Correlation, using lines of best fit and interpolation/ extrapolation

# UNIT 23 Reasoning

- I. Algebraic arguments algebraic proof and recurring decimal proof
- 2. Using angle and shape facts to derive results and circle theorems
- 3. Coordinates (including midpoints, coordinate problems)
- 4. Equations of paralleland equations of perpendicular lines5. Vectors and vector proofs

#### **UNIT 24**

#### **Geometry and Number**

- 1. Further surface area and volume (including exact answers) and similar areas and volumes
  - 2. Solve problems involving compound units
    - 3. Trigonometry in all triangles
- 4. Limits of accuracy and upper and lower bounds

#### **UNIT 25**

### **Applications of Algebra**

- I. Expand/factorise binomials and triple brackets
  - 2. Algebraic fractions
- 3. Quadratic equations; roots of functions, solving by factorising, complete the square, quadratic formula, quadratic inequalities
  - 4. Quadratic Simultaneous eqns
- 5. Cubic/reciprocal graphs, exponential graphs, trig graphs, transformations of graphs6. Graphical solutions of equations

# UNIT 26 Algebra and Geometry

- I. Arcs and sectors of circles
- 2. Proof in algebra and geometry and equation of a circle and the tangent to a circle
  - 3. Rates of change and gradients of chords and tangents
- 4. Area under a graph and interpreting in context

# **UNIT 27**

### **Revision & extension**

 Functions – will be taught at every appropriate opportunity (e.g. algebraic notation, rearranging formulae, linear graphs, mappings etc.) and then brought together as a topic here