# Curriculum Progression Pathway

# **MATHS**



#### **MATHEMATICS**

#### Why is the study of MATHEMATICS important?

MATHEMATICS has two disciplines: Pure and Applied – Pure Mathematics is the abstract science of number, quantity and space as abstract concepts and Applied Mathematics is where the knowledge learned is applied to other disciplines such as statistics, physics and engineering.

Initially your mathematics study focuses on building firm foundations, including your fluency and understanding in readiness for your future GCSE and even A level mathematics study. Our curriculum is carefully designed to ensure that all students get a firm grounding in the basic rules of number. This is differentiated by depth, as opposed to students racing onto the next topic. This approach develops more confident mathematicians as students move through the curriculum and helps them to retain their new learning for longer. Your study of mathematics at Outwood will make you think about the beauty of how numbers connect and how processes relate to each other. Mathematics encourages you to discover those connections for yourself, to make you a detective of mathematics and to explore how to solve problems. This enables you to become an analytical thinker, someone who sees that the answer is only the beginning. It will help you to learn how to make conjectures (a conclusion based on evidence, patterns and thought, but not yet confirmed with proof) to reason and to prove. It will enable you to be more logical in your approach to complex issues and be more analytical.

You will discover how the basic four rules can be applied to fractions, decimals, standard form and algebra and how multiplicative reasoning can be applied to many areas of maths, such as percentages, ratio, proportion and enlargement to name but a few. You will get to investigate the beauty of mathematics connected to shape, and the usefulness it brings in analysing data and solving mechanical problems.

Your study of Mathematics will encourage you to think deeply and help you to problem solve more effectively – a great life skill that all universities and employers will appreciate. Across your study you will explore number, algebra, shape and space and statistics. Lessons will provide a wide range of opportunities for constructing your own learning and discovering your own rules, through the use of concrete materials such as counters, through pictorial representations to demonstrate mathematical concepts and to apply these to solve problems, both abstract and from real-life.

Maths lessons will be full of discussion, questioning, proving and explaining. You are going to love it! Mathematics will expand your mind!



Big Questions such as: How tiny is the earth in comparison with the universe? How can solutions to difficult engineering problems be found using graphs and calculus? How do people predict what is going to happen in the economy? and other such seemingly bewildering questions will be answered ... you just need to learn the basics, be an inquisitive learner, and the rest will follow.

#### What skills will the study of Mathematics teach you?

You are a citizen in this world and you need to know the basic skills of number and how to apply them to a range of problems - known as 'being numerate'. It will teach you:

- Not to be afraid of "being lost" and having to struggle to find one's way through the problem RESILIENCE!
- To use calculation to solve basic problems
- To make and use generalisations—often quite quickly. One of the basic abilities, easily detectable even at the level of primary school: after solving a single example from a series, a child immediately knows how to solve all examples of the same kind.
- To have rapid and sound memorisation of mathematical material.
- To be able to concentrate on mathematics for long periods without apparent signs of tiredness.
- To be able to offer and use multiple representations of the same mathematical object. (For example, switching easily between representations of the same function by tables, charts, graphs, and analytic expressions.)
- An instinctive tendency to approach a problem in different ways: even if a problem has been already solved, you are keen to find an alternative solution.
- To utilise analogies and make connections.
- Skills to link two (or more) elementary procedures to construct a solution to a multi-step problem.
- To recognise what it means to "know for certain".
- To detect unstated assumptions in a problem, and either to explicate and utilise them, or to reject the problem as ill-defined.
- To be efficient, a distinctive tendency for "economy of thought," striving to find the most economical ways to solve problems, for clarity and simplicity in a solution.
- To be aware of the presence and importance of an underlying structure.
- To use rapid abbreviation, compression or a curtailment of reasoning in problem solving e.g. algebra.
- How to grasp encapsulation and de-encapsulation of mathematical objects and procedures.

# How does your study of MATHEMATICS support your study in other subjects?

Study of any subject in our curriculum takes full advantage of links with other subject areas- we term these as interdisciplinary links and we make the most of them because we know that deep learning requires the transference of knowledge and skills from one topic of learning to another. Once you can transfer your learning across topics and subject areas then you are really mastering what you know and how to apply your understanding and skills.

Mathematics touches on many other subjects such as geography and science, any subject that analyses data, looks at trends, uses formulae. Computer Science is a subject that uses the algorithmic approach that many topics in mathematics also use. The ability to follow a process accurately is applicable to many other subjects too. The Social Sciences, particularly at Post 16 and at undergraduate level have a strong need for the use of data, for understanding of exponential growth and decay, for manipulation of formulae – and this is one reason why the Core Maths AS Level was introduced recently.

Across the other subjects, teachers will make reference to your learning in Maths and this will help you to develop your understanding. There may be opportunities to explore the links between science, engineering and mathematics departments in STEM activities.

Outside of Mathematics lessons there are a range of initiatives that can help you deepen your understanding of mathematics such Numeracy Ninjas, Timetable Rock Stars, UKMT Maths Challenge led by Leeds University, Maths Masters – for our elite mathematicians, and online learning programmes.

#### How are you assessed in MATHEMATICS?

Throughout the 5 year MATHEMATICS course you are assessed using the following assessment objectives which ensure that you can cumulatively build your subject understanding in preparation for future GCSE and A Level study. There are half termly assessment points each year that we term Praising Stars©. For younger years we base our assessment on our subject mapping of the age related expectations across the curriculum, assessing students' performance at their current stage of study against expectation. At GCSE we make informed predictions informed by our holistic assessment of their progress against the key assessment objectives and their aspirational GCSE targets. These are also the basis for any appropriate support and intervention.

### **Key Assessment Objectives**

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# AOI: Use and apply standard techniques

Students should be able to:

- accurately recall facts, terminology and definitions
- use and interpret notation correctly
- accurately carry out routine procedures or set tasks requiring multi-step solutions

#### AO2: Reason, interpret and communicate mathematically

Students should be able to:

- · make deductions, inferences and draw conclusions from mathematical information
- construct chains of reasoning to achieve a given result
- interpret and communicate information accurately
- present arguments and proofs
- assess the validity of an argument and critically evaluate a given way of presenting information

#### AO3: Solve problems within mathematics and in other contexts

Students should be able to:

- translate problems in mathematical or non-mathematical contexts into a process or a series of mathematical processes
- make and use connections between different parts of mathematics
- interpret results in the context of the given problem
- evaluate methods used and results obtained
- evaluate solutions to identify how they may have been affected by assumptions made

#### GCSE specifications in mathematics should enable students to:

- 1. develop fluent knowledge, skills and understanding of mathematical methods and concepts
- 2. acquire, select and apply mathematical techniques to solve problems
- 3. reason mathematically, make deductions and inferences and draw conclusions
- 4. comprehend, interpret and communicate mathematical information in a variety of forms appropriate to the information and context.

#### How can Mathematics support your future?

We offer the study of GCSE Mathematics and we strongly encourage your continued study in this fantastic subject if you have demonstrated a passion for it, a flair and an ability.

However, whether you have chosen to study Mathematics into A level or not you will have gained a lot from its study over the 5 years from years 7-11. We know that the depth of understanding we encourage and support you to achieve will set you up well to be not only numerate, but a really logical and analytical thinker, who is resilient and ready to solve problems.

Mathematics is offered at prestigious universities either as a single honours or a joint honours subject studied alongside other disciplines e.g. Statistics, Computer Science, Science, Philosophy, Engineering.

A high level of qualification in mathematics is a prerequisite for honours degrees in many engineering and physics related subjects.

It is also cited that an A level in maths demonstrates the very high level of analytical thinking that many universities are looking for in their applicants. The very fact that you have been able to study mathematical thinking post 16 will help your future applications, be they for colleges, universities, apprenticeships or employment.

A strong GCSE in Maths opens doors for your future career – employers look favourably on this and it would put you in a very strong position when looking for jobs or placements Post 16 and in colleges.

Careers that the study of MATHEMATICS supports include:

- Actuarial analyst
- Actuary
- Chartered accountant
- Chartered certified accountant
- Data analyst
- Data scientist
- Investment analyst
- Research scientist (maths)
- Secondary school teacher
- Software engineer
- Statistician
- Civil Service fast streamer
- Financial manager
- Financial trader
- Insurance underwriter
- Meteorologist
- Operational researcher
- Quantity surveyor
- Software tester

# CURRICULUM PROGRESSION PATHWAY FOR MATHEMATICS AT OUTWOOD ACADEMY RIVERSIDE

|        | 1   | I  |                        |  | I            | I  | ı   | I  | I  |                                  |                                      |                       |    |
|--------|---|--|------------------------|--|--------------|--|---|--|--|----------------------------------|--------------------------------------|-----------------------|----|
| Year 7 | I   | 2  | 3                      | 4  | 5            | 6  | 7   | 8  | 9  | 10                               | П                                    | 12                    | 13 |
| Autumn | Alge<br>Genera  | bra I<br>alisation   | Baseline<br>Assessment | Proportion I<br>Multiplicative reasoning<br>Interpreting pie charts  |              | Number I Place value and powers of 10 Types of number, factors and multiples Basic HCF & LCM and primes Addition and subtraction of decimals |   | Proportion 2<br>Measurement and decimals |  | Revise,<br>Assess and<br>Respond | Displaying data incl. scatter graphs |                       | •  |
| Spring | Number 2<br>Addition and<br>subtraction of<br>fractions                           | Sha<br>Lines, angles a   |                        | I ' I and division I   |              |  | Shape 3 Area  Proportion 3 Equivalence, conversion and ordering of fractions, decimals and percentages  Proportion 3 Equivalence, Addition subtractions, decimals and percentages |  |  | Revise,<br>Assess and<br>Respond | Data 2<br>Averages and the range     |                       |    |
| Summer | Number 5 Types of number Product of prime factors HCF and LCM using Venn diagrams | Number 6<br>Multiplication<br>and division<br>of negative<br>numbers | Simplifying in         | Algebra 2<br>der of operation<br>ncl. expanding l<br>orising express | brackets and | Proportion 4 Percentage of amounts Percentage increase and decrease incl. using a multiplier   | Revise, Asses   | s and Respond                            | Algebra 3<br>Substitution and solving equations w<br>unknown on one side |                                  |                                      | Data 3<br>Probability |    |

| Year 8     | I  | 2  |    | 3  | 4          | 1   |                     | 5   | 6   | 7  | {                  | 3                          |                                    | 9      | 10  |  | П   |   | 12                         |
|------------|--|--|----|--|------------|---|---------------------|---|---|--|--------------------|----------------------------|------------------------------------|--------|---|--|---|---|----------------------------|
| Autumn     | Data 3 Probab  | bility   | Pr | ortion I Ratio<br>oportion 5<br>and proportion | Ro<br>e    | Number<br>ounding a<br>estimatin  | ınd<br>g            |   | Alget<br>Linear   |  |                    |                            | , Assess<br>espond                 |        | Data I Scatter Graphs Data 4 Two-way tables Venn diagrams Frequency trees |  | Shape<br>Congrue<br>Introducti<br>similari<br>Transform |   | uency<br>ction to<br>arity |
| Spring     | Shape 4<br>Congruenc<br>Introduction<br>similarity<br>Transformation | measures, rates and using the duction to time button fraction frac |    |  | fraction   | Number 8 our operations with an unknown of Changing the subject of a Substitution into scientific Expanding double brains |                     |   |   |  | formula<br>ormulae |                            | Revise, Assess and Respond Perimet |        |   | Circumference of circles and arc length Perimeter of semi-circles, |   | Numbe<br>r 9<br>Indices<br>and<br>surds |                            |
| Summe<br>r | Number 9<br>Indices and su   |  |    | Shape 6<br>Angles on paral<br>Angles in pol    | llel lines |   | Interpi<br>Pie<br>D | ortion I<br>ret Simple<br>Charts<br>ata 5<br>charts | as a percent<br>Proportion<br>and percent<br>Prop<br>Fractional a | 3 One number tage of another 4 Percentages entage change ortion 7 and percentage nange | Rev                | Revise, Assess and Respond |                                    | espond |   | Shape 7 of circles, semi-circles, -circles and compound shapes     |   | Number 10<br>Standard form              |                            |

| Year 9 | 1  | 2  | 3                              | 4  | 5  | 6   | 7  | 8   | 9   | 10  | Н  | 12   | 13                         |  |           |
|--------|--|--|--------------------------------|--|--|---|--|---|---|---|--|--|----------------------------|--|-----------|
| Autumn | Data 4<br>Two-way<br>tables<br>Venn diagrams<br>Frequency<br>trees                           | Shap<br>Congr<br>Introduction<br>Transfor          | ruency<br>to similarity        |  | Proportion 6<br>Compound measures                            |   | Gradients and<br>lin<br>Alge               | Area of circle quarter circles  |   | Shape 7<br>Area of circles, semi-circles,<br>quarter circles and compound<br>shapes |  | Sha <br>Angles in<br>Sha <br>Constr  | Polygons<br>be 8           |  |           |
| Spring | Proportion 8 Writing and simplifying ratios Combining rations Connecting ratio and fractions | Algel<br>Solve linear s<br>equations alge<br>graph | simultaneous<br>ebraically and | Data 7<br>Use of data  | rearrange, do<br>brac<br>Alge<br>Expand and fac              | rm, solve and<br>uble and triple<br>ckets<br>bra 9<br>torise quadratic<br>essions | Number 9 Fra<br>Number 10 (<br>I<br>Ration | aber 7 Error Inte<br>actional Indices a<br>Surds<br>Calculations in St<br>Number 11<br>ndices and Surd<br>alise the Denom<br>nal and negative | and Simplifying<br>tandard Form<br>s<br>ninator | Revise, Assess<br>and Respond   | Solve quadrati<br>facto<br>Plotting qua<br>Identify root | Algebra 10 uadratic equations by factorising ng quadratic graphs y roots of quadratic ations graphically |                            |  |           |
| Summer | Proportion 7 Growth and decay Proportion 9 Proportion problems Introduce inverse proportion  | Shap<br>Surface                                    |                                | Algebra II<br>Non-linear<br>sequences<br>incl. basic<br>quadratic<br>sequences | Shape 11<br>Volume of<br>cuboids,<br>prisms and<br>cylinders | Dai<br>Probability incl   | ·  |   | Shape 12<br>Similarity and trigonometry         |   | Ι Κονικο Δια   |  | Revise, Assess and Respond |  | e 4 ready |

| Year 10 | I   | 2   | 3                                | 4                                     | 5   | 6             | 7  | 8  | 9                                       | 10                            | 11   | 12   | 13 |  |
|---------|---|---|----------------------------------|---------------------------------------|---|---------------|--|--|---|-------------------------------|--|--|----|--|
| Autumn  | Algebra 12  Equations and inequalities  da                    |   |                                  | d interpreting                        | Calculations using standard form  Recurring decimal proof |               |  | Revise,<br>Assess and<br>Respond                 | Linear sin                              | ora 13<br>nultaneous<br>tions | Shape 13 Angles on parallel lines Angles in polygons Basic circle theorems |  |    |  |
| Spring  | y=mx+c (inc   | Algebra 14<br>inear graphs fro<br>:l. parallel and p<br>lines)<br>ying non-linear | erpendicular                     | incl. circles, ar<br>Worded pro<br>mo | and area<br>cs and sectors<br>oblems with                 | Solving quadr | ora 15<br>ratic equations<br>adratic graphs            | Data 10 Data Handling Scatter graphs Time series | Revise,<br>Assess and<br>Respond Volume |                               | Proportion 10<br>Compound measures<br>Real-life graphs                     |  |    |  |
| Summer  | Proportion II Contextual calculations and multi-step problems | Algebra 16<br>Algebraic<br>fractions  | Revise,<br>Assess and<br>Respond | Pythagoras'                           | Shape 16<br>Theorem and t<br>incl. 3D                     | rigonometry   | Proportion 12 Direct and inverse proportion and graphs | Shape 17<br>Bearings &<br>scale<br>diagrams      | Revise, Asses:                          | s and Respond                 |  | Proportion 13<br>Percentages incl. finance |    |  |